

**Directions:** Show all work.

1. **[5 points]** Use the binomial theorem to find a closed-form formula for  $\sum_{k=0}^n k2^k \binom{n}{k}$ .
2. **[5 points]** A party has a total of  $3n$  people, with  $n$  single people and  $2n$  people in  $n$  couples. Find a summation formula for the number of ways to select  $n$  people such that each couple has at most 1 selected person.