Name:

Directions: Solve the following problems. Give supporting work/justification where appropriate.

1. [4 parts, 1 point each] Let $A = \{1, 2\}$ and $B = \{\emptyset, (1, 2)\}$. Find the following sets.

(a) $A \times B$

(c) B^0

(b) A^2

(d) $A \times A \times B$

2. [1 point] Give an example of a set C such that C and C^3 have a common element.

3. [1 point] Let $D = \{1, 2, 3, 4\}$. Express $\{X \subseteq D \colon |D| \ge 3\}$ by listing the elements between braces.

4. [1 point] Draw a picture of $[2,3) \times (1,3]$ in the plane. Use solid lines to indicate boundaries in the set and dashed lines to indicate boundaries outside the set.

5. [6 parts, 0.5 points each] True/False. Write the entire word true or false. No justification necessary. We define:

$$A = \{1, 2, \{1, 2\}, \{\varnothing\}\} \qquad \quad B = \{1, \{1, 1\}, \varnothing\} \qquad \quad C = \{\{1\}\} \qquad \quad D = \{\varnothing\}$$

$$B = \{1, \{1, 1\}, \emptyset\}$$

$$C = \{\{1\}\} \qquad D$$

(a)
$$1 \in A$$

(c)
$$1 \subseteq E$$

(c)
$$1 \subseteq B$$
 (e) $D \in B$

(b)
$$C \in A$$

(d)
$$C \subseteq B$$

(f)
$$D \subseteq C$$