

Name: _____

Directions: Solve the following problems. Give supporting work/justification where appropriate.

1. [6 parts, 1 point each] Let the universe U be $\{1, \dots, 5\}$. Let $A = \{1, 2, 3\}$, $B = \{1, 3\}$, and $C = \{2, 3\}$. Find the following sets.

(a) $B \cap C$

(b) $C - B$

(c) $B \cup \bar{A}$

(d) $(B \times C) - (C \times B)$

(e) $\mathcal{P}(A) - \mathcal{P}(B \cup C)$

(f) $\mathcal{P}(A) - (\mathcal{P}(B) \cup \mathcal{P}(C))$

2. [1 point] Are there sets A and B such that $A \cap (A \times B)$ is nonempty? If yes, then give an example. If not, then explain why.

3. [3 parts, 1 point each] Let $A = \{(x, y) \in \mathbb{R}^2 : y \geq x\}$ and $B = \{(x, y) \in \mathbb{R}^2 : x^2 + y^2 \leq 1\}$. Sketch the following sets in the plane, using solid lines to represent boundaries that are in the set, and dashed lines/open circles to represent boundaries that are not in the set.

(a) A

(b) B

(c) $B - A$