

Name: _____

Directions: Solve the following problems. Give supporting work/justification where appropriate.

1. [**2 parts, 1 point each**] Let $A = \{1, 2, \emptyset\}$ and $B = \{5, \emptyset\}$. Find the following sets.

(a) $A \times B$

(b) B^3

2. [**1 point**] Suppose that $(1, 2) \in A \times B$ and $(2, 3) \in A \times B$. Find two more elements in $A \times B$.

3. [**3 parts, 1 point each**] Decide whether the following statements are true or false. Write the entire word true or the entire word false to indicate your answer. No explanations or justification required.

(a) $\{1, 2, 3\} \in \{1, 2, 3\}$

(b) $\{\mathbb{Q}\} \in \{\mathbb{Z}, \mathbb{Q}, \mathbb{R}\}$

(c) $\{\mathbb{Q}\} \subseteq \{\mathbb{Z}, \mathbb{Q}, \mathbb{R}\}$

4. [3 parts, 1 point each] Find the following power sets.

(a) $\mathcal{P}(\{a, b, c\})$

(b) $\mathcal{P}(\{\{1, 2\}, \{3\}\})$

(c) $\mathcal{P}(\{6, 7\} \times \{8\})$

5. [1 point] Let $A = \{1, 2, 3, 4\}$. Express the set $\{X \subseteq A : |X| \text{ is odd}\}$ by listing its elements between braces.