

Name: \_\_\_\_\_

**Directions:** Solve the following problems. Give supporting work/justification where appropriate.1. [**2 parts, 3 points each**] Prove or disprove the following.(a) Suppose that  $a, b \in \mathbb{Z}$ . If  $a \mid b$  and  $b \mid a$ , then  $a = b$ .(b) If  $n \in \mathbb{N}$ , then  $n^3 + 8$  is not prime.

2. [4 points] Prove that if  $n \in \mathbb{N}$ , then  $\sum_{k=1}^n k(k+1) = \frac{n(n+1)(n+2)}{3}$ .