

Disclaimer: the questions below only represent my best guesses as to what *might* be on the exam. I don't have any inside information. The official practice exam – once it's posted – should give a better indication of what the real thing will look like.

I have *tried* to err on the side of making the practice exam too difficult, rather than too easy. Keep that in mind.

1. Find the equation of the tangent line to the curve  $4x^2y + y^3 = 16$  at the point  $(1, 2)$ .
2. A baker wishes to make a square pizza. He begins by producing 450 cubic centimeters of dough for the crust, and rolling it flat. The baker rolls out the dough in such a way that the top of the dough remains perfectly square at all times, and the thickness decreases at a rate of 0.1 centimeters per second. When the dough is 2 centimeters thick, how quickly is its width growing?
3. Let  $f(x) = 2x^3 + 5x^2 - 4x + 73$ .
  - (a) Where is  $f(x)$  concave up? Where is it concave down?
  - (b) Find the critical points of  $f(x)$  and use the second derivative test to classify them as relative maxima or relative minima.
4. (a) Find all asymptotes of the curve  $f(x) = \frac{2x^2 - 9x + 4}{x^2 - 3x - 4}$ .  
(b) Sketch a graph of some function  $g(t)$  for which:
  - $g'(t)$  is positive on  $(-\infty, -4)$  and  $(4, \infty)$ , but negative on  $(-4, 4)$ ;
  - $g''(t)$  is positive on  $(-2, 0)$ , but negative on  $(-\infty, -2)$ ,  $(0, 4)$ , and  $(4, \infty)$ .
5. McGraw-Hill, a textbook publisher, wants to determine a price for the latest edition of their most popular calculus textbook. Their research indicates that a book priced at  $p$  dollars will sell  $D(p) = 1500000p^{-1} - 1000$  copies. Naturally, McGraw-Hill intends to produce only as many textbooks as they can sell. Textbook production incurs a flat overhead cost of \$80,000, as well as a material cost of \$15 per book. At what price should McGraw-Hill sell their calculus book in order to maximize their profits?
6. Solve for  $x$ :
  - (a)  $2^{8-x} = 4^x$
  - (b)  $2^{3x} = 24 \cdot 3^{-x}$
  - (c)  $\ln x - \ln 4 = 2(\ln 3 - \ln 2)$