

1. Find all eigenvector/eigenvalue pairs for the following matrices.

(a)  $\begin{bmatrix} 7 & 8 \\ -4 & -5 \end{bmatrix}$

(b)  $\begin{bmatrix} 4 & -3 \\ 6 & -2 \end{bmatrix}$

(c)  $\begin{bmatrix} 1 & 2 & 0 \\ 0 & -1 & 0 \\ -4 & 4 & 3 \end{bmatrix}$

2. A  $2 \times 2$  system with real values.

(a) Find the general solution to

$$\begin{aligned}x_1' &= -7x_1 + 10x_2 \\x_2' &= -5x_1 + 8x_2.\end{aligned}$$

(b) Draw a phase portrait for the system above.

(c) Find the solution with initial conditions  $x_1(0) = 1$ ,  $x_2(0) = -1$ .