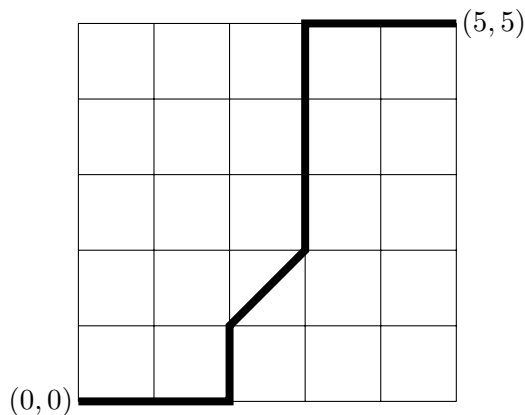


Directions: You may work to solve these problems in groups, but all written work must be your own. **Show your work;** See “Guidelines and advice” on the course webpage for more information.

1. How many 5-digit ATM pin numbers:
 - (a) have distinct digits that increase from left to right? (So 02379 counts, but 02279 and 20458 do not.)
 - (b) have digits that are non-decreasing from left to right? (So 02379 and 02279 count, but 20458 does not.)
2. *Solutions to equations.* Count the number of non-negative integral solutions to the following equations.
 - (a) $x_1 + x_2 + \cdots + x_6 = 50$
 - (b) $x_1 + x_2 + \cdots + x_6 = 50$ where each x_i is at least 4
 - (c) $x_1 + x_2 + \cdots + x_6 = 50$ where $x_1 \leq 20$
 - (d) $x_1 + x_2 + \cdots + x_6 = 50$ where $1 \leq x_i \leq 30$ for all i .
3. *Lattice paths with diagonal steps.* A *diagonal step* in a lattice path moves 1 unit in the x -direction and 1-unit in the y direction.



- (a) For each k with $0 \leq k \leq 5$, determine the number of lattice paths with diagonal steps from $(0,0)$ to $(5,5)$ that have exactly k diagonal steps. (A lattice path from $(0,0)$ to $(5,5)$ with 1 diagonal step is displayed above.)
- (b) Add your results from part (a) to determine the total number of lattice paths from $(0,0)$ to $(5,5)$ with diagonal steps.
- (c) Using Σ notation, give a summation formula for the number of lattice paths with diagonal steps from $(0,0)$ to (n,n) .