

Name: _____

1. **[2.5 points]** Solve the initial value problem $y'' + 8y' - 9y = 0$ with $y(0) = 1$ and $y'(0) = 2$. Express your answer using real numbers only.

2. **[2.5 points]** Find the general solution to $y'' + 2y' + 2y = 0$. Express your answer using real numbers only.

3. [1 point] Short answer. Suppose that y_1 and y_2 are solutions to $y'' + p(t)y' + q(t) = 0$ on an open interval I . What useful information does the Wronskian of y_1 and y_2 provide?

4. [2 points] Compute the Wronskian of $\sin t$ and $t \sin t$.

5. [2 points] Solve the following differential equation: $x \frac{dy}{dx} + xy = 1 - y$.